

1) Suppose particle 1 with a charge of  $-80 \mu\text{C}$  is located at  $x = 0$  on an x-axis, and particle 2 with a charge of  $+20 \mu\text{C}$  is located at  $x = 20 \text{ cm}$ . Where would I have to place a third particle with a charge of  $+20 \mu\text{C}$  such that the total force on the third charge is zero?

**Solution:** We are looking for a spot where the electric field from particles 1 and 2 is zero, which means that the charge on the third particle does not matter. I just threw that in so as to cause confusion.

Charge 3 cannot be between charges 1 and 2, because in that region their electric fields are both in the same direction and cannot cancel. It cannot be in the region of  $x < 0$  because charge 1 is greater than charge 2, so charge 2 (which is farther away) can never cancel charge 1 there.

Thus charge 3 is in the region  $x > 20 \text{ cm}$ . One can quickly get the distance where  $F = 0$  by recognizing that charge 1 is exactly four times the magnitude of charge 2, so charge 1 needs to be exactly twice as far from charge 3 as charge 2 is from charge 3 for cancellation to occur. This is true at  $x = 40 \text{ cm}$ .

Alternatively, you can be more mathematical and set  $kq_1 / x^2 + kq_2 / (x - 20)^2 = 0$ , where “x” is the unknown distance of charge 3. (It is OK to use cm instead of meters because the units cancel out.) A little algebra yields  $4(x - 20)^2 = x^2$ , or  $2(x - 20) = x$ , or  $x = 40 \text{ cm}$ .

- 2) Suppose that an electric dipole has charges  $+3e$  and  $-3e$  separated by  $0.68 \text{ nm}$ , and is oriented along the positive  $i$  (or x) axis with its negative charge to the left (positive charge to the right). Then an electric field with  $\mathbf{E} = 4000 \text{ N/C } i + 3000 \text{ N/C } j$  is placed across the dipole.
- At what new angle (relative to the x-axis) will the dipole try to point?
  - How much kinetic energy will the dipole gain or lose as it rotates to the angle in part (a)?

**Solution:** The dipole will try to rotate to lie along the electric field. The angle of the electric field is given by  $\tan\theta = 3/4$ , or  $\theta = 36.9^\circ$

The dipole will gain rotational kinetic energy as it spins into its new position. We have:  
 $U = pE \cos\theta = (0.68 \text{ nm})(3e)(5000 \text{ N/C}) \cos(36.9^\circ) = 1.3 \times 10^{-24} \text{ J}$  as the magnitude of the initial potential energy of the dipole. When it is aligned with the field,  $\cos\theta = 1$ , so its energy in that state will be  $(0.68 \text{ nm})(3e)(5000 \text{ N/C})(1) = 1.63 \times 10^{-24} \text{ J}$ . The difference in potential will show up as kinetic energy, so  $\Delta U = 1.63 \times 10^{-24} \text{ J} - 1.3 \times 10^{-24} \text{ J} = 0.33 \times 10^{-24} \text{ J}$ .