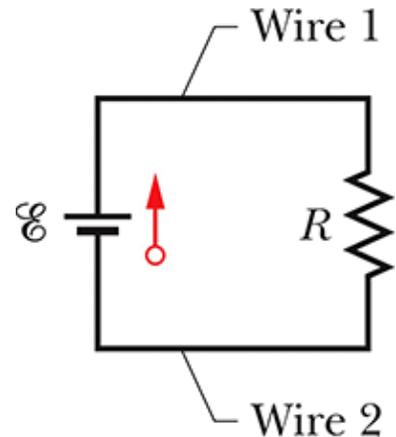


1) An ideal 9-volt battery is connected across a resistor of 10Ω . The two wires which connect the battery to the resistor are NOT ideal: they are each 1.5 m long, 0.5 mm in radius, and made of iron.



1a) (3 points) If the resistivity of iron is $9.68 \times 10^{-8} \Omega \text{ m}$, what is the resistance of each wire?

Solution: Using $R = \rho L / A$, and $A = \pi r^2$, we have:

$$R = (9.68 \times 10^{-8})(1.5) / \pi(5 \times 10^{-4})^2 = 0.185 \Omega.$$

1b) (3 points) What is the current flowing in this circuit?

Solution: From $V = iR$, we have $9 \text{ v} = i(0.185 + 10 + 0.185)$, or $i = 0.868 \text{ A}$.

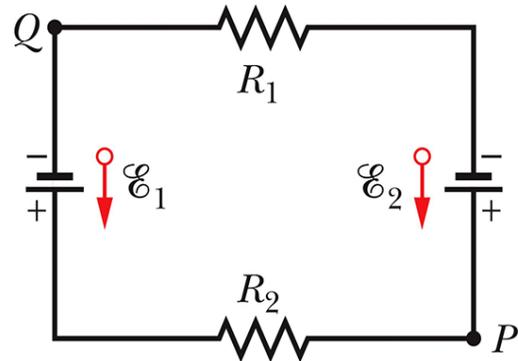
1c) (3 points) What is the total power being consumed by this circuit?

Solution: Using $P = i^2R$, we see that the total power being used is $(0.868)^2(10.37) = 7.81 \text{ W}$.

1d) (3 points) Of the total power being consumed by this circuit, what percentage of it is being “wasted” as heat energy in the iron wires?

Solution: Since $P = i^2R$, and the current is the same throughout the circuit, the fraction of the power being used by the wires is simply $(2 \times 0.185) / 10.37 = 3.6\%$.

2) (8 points) In the little circuit shown at right, suppose $\mathcal{E}_1 = 9 \text{ v}$, $\mathcal{E}_2 = 6 \text{ v}$, $R_1 = 10 \Omega$, and $R_2 = 20 \Omega$. If point P is held at ground, what will be the voltage at point Q?



Solution

The current flowing in this circuit is:

$$(9 \text{ v} - 6 \text{ v}) = i(10 + 20), \text{ or } i = 0.1 \text{ amp.}$$

There are several ways to calculate the voltage at Q.

Possibly the easiest is just to start at Q and follow the current to P. Going across the first battery raises the voltage by 9, then going across resistor 2 lowers it by $iR = 2$ volts. Thus P is at 7 volts above Q, which means that Q must be at **-7 volts** (since P is at $V = 0$).

You could also start at P, then go across battery 2. This will lower the voltage by 6 volts, because you are going backwards across the battery. You lose another volt going across resistor 1, and that places you at -7 volts, as before.