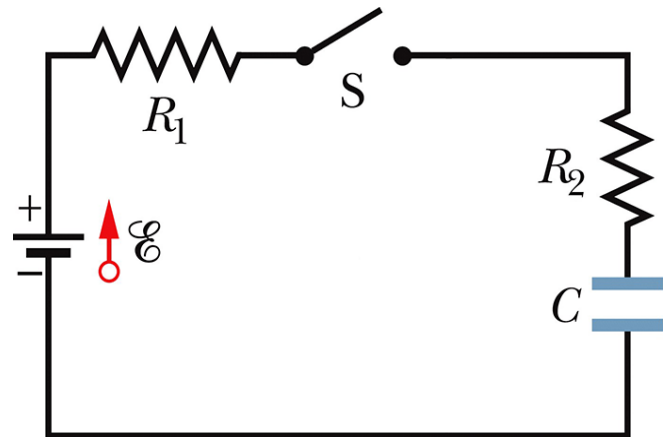


Phyx 135-2, Fall 2016, Quiz #4
Section 01 (10 am)

Name _____

1) (12 points) In the circuit at right, an ideal 9-volt battery is connected to $R_1 = 10 \text{ M}\Omega$, $R_2 = 20 \text{ M}\Omega$, and $C = 4 \text{ }\mu\text{F}$. The capacitor is uncharged. Then, the switch S is closed. At $t =$ one minute later, what will be the voltage drop across R_1 ?



Solution

The voltage across the capacitor will rise with time according to the formula:

$$V = V_0[1 - \exp(-t/RC)].$$

In this case $t = 60 \text{ sec}$, $R = 30 \text{ M}\Omega$, and $C = 4 \text{ }\mu\text{F}$, so $t / RC = 60 / 120 = 0.5$, and the voltage across the capacitor is $V = 9(1 - e^{-0.5}) = 3.54 \text{ volts}$. This voltage will *oppose* the voltage from the battery, so the voltage across R_1 and R_2 at $t = 60 \text{ s}$ is $9 - 3.54 = 5.46 \text{ v}$. Finally, since R_1 and R_2 are in series, $10 / (10 + 20) = 1/3$ of this voltage will appear across R_1 , so $V_1 = 1.82 \text{ v}$.

2) (8 points) An α -particle is a sub-atomic particle which has a mass of $6.7 \times 10^{-27} \text{ kg}$, and carries twice the charge of an electron. If an α -particle is shot into a uniform magnetic field of 2 Tesla (with v at right angles to B), and proceeds to rotate in a circle of 1 mm radius, what is the velocity of the α -particle?

Solution

From basic mechanics we know that a particle rotating in a circle in a magnetic field must have a Lorentz force acting on it that is equal to the centrifugal force, or $mv^2 / r = qvB$. This tells us that $v = qBr / m = (2)(1.6 \times 10^{-19})(2)(10^{-3}) / (6.7 \times 10^{-27}) = 9.6 \times 10^4 \text{ m/s}$.