

1) Suppose you have a 7.5 mH inductor and a 4.5  $\mu\text{F}$  capacitor connected in series. (The resistance of the circuit is zero.) The maximum charge that ever appears on the capacitor is 2.0  $\mu\text{C}$ .

1a) (4 points) What is the frequency of oscillation of this circuit, given in Hz?

Answer:  $\omega = (LC)^{-1/2} = [(7.5 \times 10^{-3})(4.5 \times 10^{-6})]^{-1/2} = 5443 \text{ rad/s}$ .  $\omega = 2\pi f$ , so  $f = 5443/2\pi = 866 \text{ Hz}$

1b) (4 points) What is the maximum current that ever flows through the inductor?

Answer:  $i_{\text{max}} = \omega q_{\text{max}} = (5443)(2 \times 10^{-6}) = 10.9 \text{ mA}$

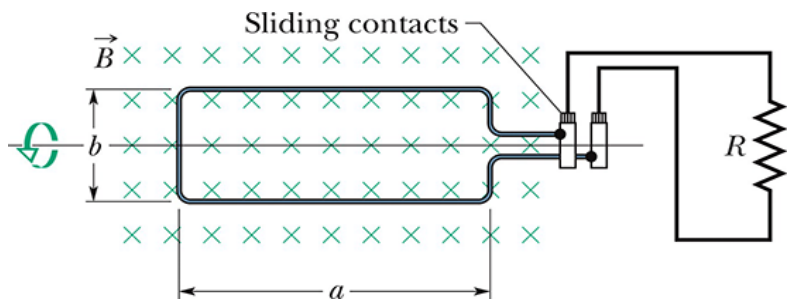
1c) (4 points) What is the total energy contained in this circuit?

Answer: We may use either  $U = \frac{1}{2} Q^2/C$  or  $U = \frac{1}{2} Li^2$ . We have:

$$U = \frac{1}{2}(2 \times 10^{-6})^2 / (4.5 \times 10^{-6}) = 0.44 \mu\text{J}, \text{ or}$$

$$U = \frac{1}{2}(7.5 \times 10^{-3})(10.9 \times 10^{-3})^2 = 0.44 \mu\text{J}$$

2) (8 points) You have a rectangular loop of wire with length  $a = 7 \text{ cm}$  and width  $b = 3 \text{ cm}$ . It is in a constant magnetic field of 0.50 T as shown at right. Then, you begin to rotate the wire around its length at a frequency of  $f = 60 \text{ Hz}$ . What is the maximum emf that will appear in the loop?



**Solution**

From Faraday's Law,  $\mathcal{E} = d\Phi/dt$ . In this case, because the loop is rotating, we have:

$\Phi = BA \cos(\omega t)$ . Thus  $d\Phi/dt = BA\omega \sin(\omega t)$ , so the maximum emf that can appear in the loop is just  $BA\omega = B(ab)(2\pi f) = (0.5)(0.07)(0.03)(2\pi)(60) = 0.4 \text{ volt}$