

58. (a) $\tau = RC = (1.40 \times 10^6 \Omega)(1.80 \times 10^{-6} \text{ F}) = 2.52 \text{ s}$.

(b) $q_0 = \varepsilon C = (12.0 \text{ V})(1.80 \mu\text{F}) = 21.6 \mu\text{C}$.

(c) The time t satisfies $q = q_0(1 - e^{-t/RC})$, or

$$t = RC \ln\left(\frac{q_0}{q_0 - q}\right) = (2.52 \text{ s}) \ln\left(\frac{21.6 \mu\text{C}}{21.6 \mu\text{C} - 16.0 \mu\text{C}}\right) = 3.40 \text{ s}.$$

62. The time it takes for the voltage difference across the capacitor to reach V_L is given by $V_L = \varepsilon(1 - e^{-t/RC})$. We solve for R :

$$R = \frac{t}{C \ln[\varepsilon/(\varepsilon - V_L)]} = \frac{0.500 \text{ s}}{(0.150 \times 10^{-6} \text{ F}) \ln[95.0 \text{ V}/(95.0 \text{ V} - 72.0 \text{ V})]} = 2.35 \times 10^6 \Omega$$

where we used $t = 0.500 \text{ s}$ given (implicitly) in the problem.

64. (a) The potential difference V across the plates of a capacitor is related to the charge q on the positive plate by $V = q/C$, where C is capacitance. Since the charge on a discharging capacitor is given by $q = q_0 e^{-t/\tau}$, this means $V = V_0 e^{-t/\tau}$ where V_0 is the initial potential difference. We solve for the time constant τ by dividing by V_0 and taking the natural logarithm:

$$\tau = -\frac{t}{\ln(V/V_0)} = -\frac{10.0 \text{ s}}{\ln[(1.00 \text{ V})/(100 \text{ V})]} = 2.17 \text{ s}.$$

(b) At $t = 17.0 \text{ s}$, $t/\tau = (17.0 \text{ s})/(2.17 \text{ s}) = 7.83$, so

$$V = V_0 e^{-t/\tau} = (100 \text{ V})e^{-7.83} = 3.96 \times 10^{-2} \text{ V}.$$

65. In the steady state situation, the capacitor voltage will equal the voltage across $R_2 = 15 \text{ k}\Omega$:

$$V_0 = R_2 \frac{\varepsilon}{R_1 + R_2} = (15.0 \text{ k}\Omega) \left(\frac{20.0 \text{ V}}{10.0 \text{ k}\Omega + 15.0 \text{ k}\Omega} \right) = 12.0 \text{ V}.$$

Now, multiplying Eq. 27-39 by the capacitance leads to $V = V_0 e^{-t/RC}$ describing the voltage across the capacitor (and across $R_2 = 15.0 \text{ k}\Omega$) after the switch is opened (at $t = 0$). Thus, with $t = 0.00400 \text{ s}$, we obtain

$$V = (12)e^{-0.004/(15000)(0.4 \times 10^{-6})} = 6.16 \text{ V}.$$

Therefore, using Ohm's law, the current through R_2 is $6.16/15000 = 4.11 \times 10^{-4} \text{ A}$.