

35. Equation 29-13 gives the magnitude of the force between the wires, and finding the  $x$ -component of it amounts to multiplying that magnitude by  $\cos\phi = \frac{d_2}{\sqrt{d_1^2 + d_2^2}}$ . Therefore, the  $x$ -component of the force per unit length is

$$\begin{aligned}\frac{F_x}{L} &= \frac{\mu_0 i_1 i_2 d_2}{2\pi(d_1^2 + d_2^2)} = \frac{(4\pi \times 10^{-7} \text{ T} \cdot \text{m/A})(4.00 \times 10^{-3} \text{ A})(6.80 \times 10^{-3} \text{ A})(0.050 \text{ m})}{2\pi[(0.0240 \text{ m})^2 + (0.050 \text{ m})^2]} \\ &= 8.84 \times 10^{-11} \text{ N/m}.\end{aligned}$$

36. We label these wires 1 through 5, left to right, and use Eq. 29-13. Then,

(a) The magnetic force on wire 1 is

$$\begin{aligned}\vec{F}_1 &= \frac{\mu_0 i^2 l}{2\pi} \left( \frac{1}{d} + \frac{1}{2d} + \frac{1}{3d} + \frac{1}{4d} \right) \hat{j} = \frac{25\mu_0 i^2 l}{24\pi d} \hat{j} = \frac{25(4\pi \times 10^{-7} \text{ T} \cdot \text{m/A})(3.00 \text{ A})^2 (10.0 \text{ m})}{24\pi(8.00 \times 10^{-2} \text{ m})} \hat{j} \\ &= (4.69 \times 10^{-4} \text{ N}) \hat{j}.\end{aligned}$$

(b) Similarly, for wire 2, we have

$$\vec{F}_2 = \frac{\mu_0 i^2 l}{2\pi} \left( \frac{1}{2d} + \frac{1}{3d} \right) \hat{j} = \frac{5\mu_0 i^2 l}{12\pi d} \hat{j} = (1.88 \times 10^{-4} \text{ N}) \hat{j}.$$

(c)  $F_3 = 0$  (because of symmetry).

(d)  $\vec{F}_4 = -\vec{F}_2 = (-1.88 \times 10^{-4} \text{ N}) \hat{j}$ , and

(e)  $\vec{F}_5 = -\vec{F}_1 = -(4.69 \times 10^{-4} \text{ N}) \hat{j}$ .

44. We use Ampere's law:  $\oint \vec{B} \cdot d\vec{s} = \mu_0 i$ , where the integral is around a closed loop and  $i$  is the net current through the loop.

(a) For path 1, the result is

$$\oint_1 \vec{B} \cdot d\vec{s} = \mu_0 (-5.0 \text{ A} + 3.0 \text{ A}) = (4\pi \times 10^{-7} \text{ T} \cdot \text{m/A})(-2.0 \text{ A}) = -2.5 \times 10^{-6} \text{ T} \cdot \text{m}.$$

(b) For path 2, we find

$$\oint_2 \vec{B} \cdot d\vec{s} = \mu_0 (-5.0 \text{ A} - 5.0 \text{ A} - 3.0 \text{ A}) = (4\pi \times 10^{-7} \text{ T} \cdot \text{m/A})(-13.0 \text{ A}) = -1.6 \times 10^{-5} \text{ T} \cdot \text{m}.$$

48. (a) The field at the center of the pipe (point  $C$ ) is due to the wire alone, with a magnitude of

$$B_C = \frac{\mu_0 i_{\text{wire}}}{2\pi(3R)} = \frac{\mu_0 i_{\text{wire}}}{6\pi R}.$$

For the wire we have  $B_{P, \text{wire}} > B_{C, \text{wire}}$ . Thus, for  $B_P = B_C = B_{C, \text{wire}}$ ,  $i_{\text{wire}}$  must be into the page:

$$B_P = B_{P, \text{wire}} - B_{P, \text{pipe}} = \frac{\mu_0 i_{\text{wire}}}{2\pi R} - \frac{\mu_0 i}{2\pi(2R)}.$$

Setting  $B_C = -B_P$  we obtain  $i_{\text{wire}} = 3i/8 = 3(8.00 \times 10^{-3} \text{ A})/8 = 3.00 \times 10^{-3} \text{ A}$ .

(b) The direction is into the page.