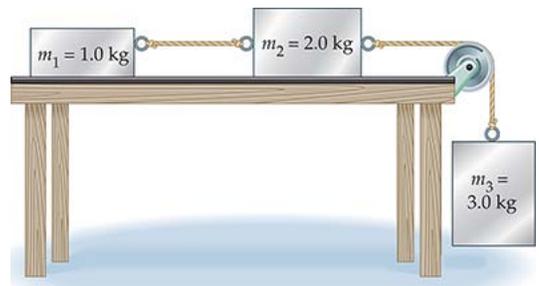


1) (12 points) Two masses of 1.0 kg and 2.0 kg are setting on a table, as shown at right. Both masses have  $\mu = 0.25$  for their coefficient of kinetic friction. A hanging mass of 3 kg is attached to them by a cord. What are the tensions in the two cords?



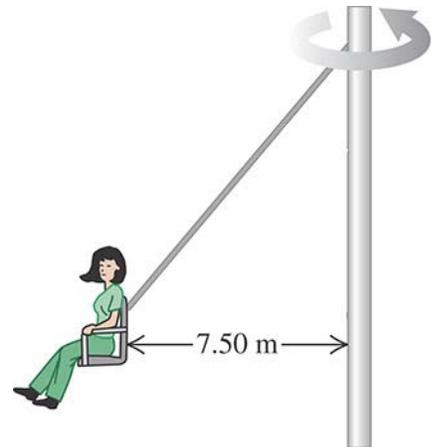
**Solution**

The total frictional force acting on the two masses is just  $F = \mu N = (0.25)(1 + 2)(9.8) = 7.35 \text{ N}$ . This will oppose the force being applied by the 3 kg mass, so the acceleration of the system is given by:  $(3)(9.8) - 7.35 = (1 + 2 + 3)a$ , or  $a = 3.675 \text{ m/s}^2$ .

The first string (the one on the left) only has to accelerate the first mass. So, it will supply a tension of  $ma + \mu N = (1)(3.675) + (0.25)(1)(9.8) = 6.125 \text{ N}$ .

The second string must accelerate both masses, so it will supply a tension of  $ma + \mu N = (3)(3.675) + (0.25)(3)(9.8) = 18.375 \text{ N}$ .

2) (8 points) The girl at right is sitting on a seat at the end of a rope. She rotating around a pole on a carnival ride at a rate of one revolution every 4 seconds. She has a mass of 50 kg. What is the tension in the rope?



**Solution**

There are two “forces” acting on her. One is gravity, which acts straight down. This is  $mg = (50)(9.8) = 490 \text{ N}$ . The other “force” is the centrifugal force of her rotation, which is acting directly outwards from the pole, i.e., at  $90^\circ$  to the gravity. Since she is rotating once every four seconds, her rotation frequency is 0.25 cycles per second. This gives us  $F = m\omega^2 r = m(2\pi f)^2 r = (50)(2\pi \cdot \frac{1}{4})^2 (7.5) = 925 \text{ N}$ . The Pythagorean Theorem then gives us the total force acting on her, which must also be the tension in the rope:  $(490^2 + 925^2)^{1/2} = 1047 \text{ N}$ .