

14. (a) For the maximum adjacent to the central one, we set $m = 1$ in Eq. 35-14 and obtain

$$\theta_1 = \sin^{-1} \left(\frac{m\lambda}{d} \right) \Big|_{m=1} = \sin^{-1} \left[\frac{(1)(\lambda)}{100\lambda} \right] = 0.010 \text{ rad.}$$

(b) Since $y_1 = D \tan \theta_1$ (see Fig. 35-10(a)), we obtain

$$y_1 = (500 \text{ mm}) \tan (0.010 \text{ rad}) = 5.0 \text{ mm.}$$

The separation is $\Delta y = y_1 - y_0 = y_1 - 0 = 5.0 \text{ mm}$.

15. The angular positions of the maxima of a two-slit interference pattern are given by $d \sin \theta = m\lambda$, where d is the slit separation, λ is the wavelength, and m is an integer. If θ is small, $\sin \theta$ may be approximated by θ in radians. Then, $\theta = m\lambda/d$ to good approximation. The angular separation of two adjacent maxima is $\Delta\theta = \lambda/d$. Let λ' be the wavelength for which the angular separation is greater by 10.0%. Then, $1.10\lambda/d = \lambda'/d$. or

$$\lambda' = 1.10\lambda = 1.10(589 \text{ nm}) = 648 \text{ nm.}$$

20. (a) We use Eq. 35-14 with $m = 3$:

$$\theta = \sin^{-1} \left(\frac{m\lambda}{d} \right) = \sin^{-1} \left[\frac{2(550 \times 10^{-9} \text{ m})}{7.70 \times 10^{-6} \text{ m}} \right] = 0.216 \text{ rad.}$$

(b) $\theta = (0.216) (180^\circ/\pi) = 12.4^\circ$.

26. (a) We use Eq. 35-14 to find d :

$$d \sin \theta = m\lambda \quad \Rightarrow \quad d = (4)(450 \text{ nm})/\sin(90^\circ) = 1800 \text{ nm} .$$

For the third order spectrum, the wavelength that corresponds to $\theta = 90^\circ$ is

$$\lambda = d \sin(90^\circ)/3 = 600 \text{ nm} .$$

Any wavelength greater than this will not be seen. Thus, $600 \text{ nm} < \theta \leq 700 \text{ nm}$ are absent.

(b) The slit separation d needs to be decreased.

(c) In this case, the 400 nm wavelength in the $m = 4$ diffraction is to occur at 90° . Thus

$$d_{\text{new}} \sin \theta = m\lambda \quad \Rightarrow \quad d_{\text{new}} = (4)(400 \text{ nm})/\sin(90^\circ) = 1600 \text{ nm} .$$

This represents a change of

$$|\Delta d| = d - d_{\text{new}} = 200 \text{ nm} = 0.20 \text{ } \mu\text{m}.$$