

4. Due to the time-dilation effect, the time between initial and final ages for the daughter is longer than the four years experienced by her father:

$$t_{f \text{ daughter}} - t_{i \text{ daughter}} = \gamma(4.000 \text{ y})$$

where  $\gamma$  is Lorentz factor (Eq. 37-8). Letting  $T$  denote the age of the father, then the conditions of the problem require

$$T_i = t_{i \text{ daughter}} + 20.00 \text{ y}, \quad T_f = t_{f \text{ daughter}} - 20.00 \text{ y} .$$

Since  $T_f - T_i = 4.000 \text{ y}$ , then these three equations combine to give a single condition from which  $\gamma$  can be determined (and consequently  $v$ ):

$$44 = 4\gamma \Rightarrow \gamma = 11 \Rightarrow \beta = \frac{2\sqrt{30}}{11} = 0.9959.$$

5. In the laboratory, it travels a distance  $d = 0.00105 \text{ m} = vt$ , where  $v = 0.992c$  and  $t$  is the time measured on the laboratory clocks. We can use Eq. 37-7 to relate  $t$  to the proper lifetime of the particle  $t_0$ :

$$t = \frac{t_0}{\sqrt{1-(v/c)^2}} \Rightarrow t_0 = t \sqrt{1-\left(\frac{v}{c}\right)^2} = \frac{d}{0.992c} \sqrt{1-0.992^2}$$

which yields  $t_0 = 4.46 \times 10^{-13} \text{ s} = 0.446 \text{ ps}$ .