

51. (a) Setting $\lambda = h / p = h / \sqrt{(E/c)^2 - m_e^2 c^2}$, we solve for $K = E - m_e c^2$:

$$K = \sqrt{\left(\frac{hc}{\lambda}\right)^2 + m_e^2 c^4} - m_e c^2 = \sqrt{\left(\frac{1240 \text{ eV} \cdot \text{nm}}{10 \times 10^{-3} \text{ nm}}\right)^2 + (0.511 \text{ MeV})^2} - 0.511 \text{ MeV}$$

$$= 0.015 \text{ MeV} = 15 \text{ keV}.$$

(b) Using the value $hc = 1240 \text{ eV} \cdot \text{nm}$

$$E = \frac{hc}{\lambda} = \frac{1240 \text{ eV} \cdot \text{nm}}{10 \times 10^{-3} \text{ nm}} = 1.2 \times 10^5 \text{ eV} = 120 \text{ keV}.$$

(c) The electron microscope is more suitable, as the required energy of the electrons is much less than that of the photons.

53. The wavelength associated with the unknown particle is

$$\lambda_p = \frac{h}{p_p} = \frac{h}{m_p v_p},$$

where p_p is its momentum, m_p is its mass, and v_p is its speed. The classical relationship $p_p = m_p v_p$ was used. Similarly, the wavelength associated with the electron is $\lambda_e = h / (m_e v_e)$, where m_e is its mass and v_e is its speed. The ratio of the wavelengths is

$$\lambda_p / \lambda_e = (m_e v_e) / (m_p v_p),$$

so

$$m_p = \frac{v_e \lambda_e}{v_p \lambda_p} m_e = \frac{9.109 \times 10^{-31} \text{ kg}}{3(1.813 \times 10^{-4})} = 1.675 \times 10^{-27} \text{ kg}.$$

According to Appendix B, this is the mass of a neutron.

63. If the momentum is measured at the same time as the position, then

$$\Delta p \approx \frac{h}{\Delta x} = \frac{6.63 \times 10^{-34} \text{ J} \cdot \text{s}}{2\pi(50 \text{ pm})} = 2.1 \times 10^{-24} \text{ kg} \cdot \text{m/s}.$$

74. (a) The average kinetic energy is

$$K = \frac{3}{2} kT = \frac{3}{2} (1.38 \times 10^{-23} \text{ J / K})(300 \text{ K}) = 6.21 \times 10^{-21} \text{ J} = 3.88 \times 10^{-2} \text{ eV}.$$

(b) The de Broglie wavelength is

$$\lambda = \frac{h}{\sqrt{2m_n K}} = \frac{6.63 \times 10^{-34} \text{ J} \cdot \text{s}}{\sqrt{2(1.675 \times 10^{-27} \text{ kg})(6.21 \times 10^{-21} \text{ J})}} = 1.46 \times 10^{-10} \text{ m}.$$